

Am I Ready to Contemplate Infinity with Algebra?

These questions are meant to help you gauge your readiness for Non-Euclidean Geometry. Getting the correct answers (which are on the last page) is a good, using a method that works in additional cases is better, but understanding *why* is the gold standard, and one that only you can assess. If you need to use technology to answer these questions, you are probably not a good fit (computers and calculators do not handle infinity well!).

- 1. Expand the following products:
 - (a) $(x^2 + 3x + 2)(2x^3 5x + 1)$
 - (b) $(x^2 + x + 1)^3$

2. Simplify:

$$\frac{3x^3 + 4x^2 + x + 10}{x + 2}$$

- 3. Let $f(x) = \sqrt{x+5}$ and $g(x) = x^2 9$.
 - (a) Evaluate $(f \circ g)(x)$ and state the domain.
 - (b) Evaluate $(g \circ f)(x)$ and state the domain.

- 4. Solve for all real values of x:
 - (a) $\log(x-4) = 1 \log(x-1)$
 - (b) $x = \sqrt{x+7} + 5$



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Answers:

1. (a)
$$2x^5 + 6x^4 - x^3 - 14x^2 - 7x + 2$$

(b)
$$x^6 + 3x^5 + 6x^4 + 7x^3 + 6x^2 + 3x + 1$$

2.
$$3x^2 - 2x + 5$$
 for $x \neq -2$

3. (a)
$$(f \circ g)(x) = \sqrt{x^2 - 4}, x \in [-2, 2]$$

4. (a)
$$x = -1$$
 (note: $x \neq 6$)

(b
$$(g \circ f)(x) = x - 4, x \in \mathbb{R}$$

(b) $x = 9$ (note: $x \neq 2$)